

# Personal Selection Problem in Group Decision Making Method VIA Bipolar Uncertainty Structure

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# ABSTRACT

In this paper, we investigate personal selection problem by using group decision making aspect through bipolar uncertainty structures. we use the score function and accuracy functions and the hybrid score-accuracy functions of bipolar fuzzy soft numbers (BFSNS) and ranking method for BFSNS. Also we analyse to the degree of grey relations among all professors and  $BF\alpha IS$  and  $BF\beta IS$  is calculated. Comparison is also evaluated for effectiveness of the appointment.

Keywords: Soft set, bipolar Fuzzy soft set (BFSS), bipolar fuzzy soft number (BFSN) Decision making, hybrid score and accuracy function.

# INTRODUCTION

Recruitment process can be regarded as a multi-criteria group decision making (MCGDM) problem that generally consists of the selection of the most desirable alternative from all the feasible alternatives. Classical MCGDM approaches [1,5,9] deal with non fuzzy numbers that is the ratings and the weights of criteria are measured by crisp numbers. However, to present the information by crisp numbers isnot always possible. The fuzzy sets introduces by Zadeh in 1965 [18] can be usedin order to deal this situation. Compared to a fuzzy set a bipolar approach is more general and suitable way to deal with imprecise information, Bosc and Pivert [3] said that "Bipolarity refers to the propensity of the human mind to reason and make decisions on the basis of positive and negative effects and the positive information states what is possible, satisfactory, permitted, desired, or considered as being acceptable. Whereas the negative statements express what is impossible, rejected or forbidden. Thus, Lee [[12],[13]]has introduced the concept of bipolar fuzzy sets which is a generalization of the fuzzy sets. At recent times, many authors or algebraic structures study the bipolar fuzzy models.J.Chen.al [4] has studied the m-polar fuzzy set and has illustrated how many concepts have been defined on bipolar fuzzy sets. Many results have been examined, related to these concepts which can be generalized to the case of m-polar fuzzy sets.

To show how to apply m-polar fuzzy sets in real world problems, numerical examples are also being proposed. P.Bosc and O.Pivert [3] has introduced a study called the bipolar fuzzy relations where each tuple associates with a pair of satisfactory degrees, bipolar value fuzzy [1,2] – ideal and bipolar valued fuzzy ideal. M. Zhou and S.Li [17] has introduced a new frame work of bipolar fuzzy set semi rings and bipolar fuzzy ideals which is a generalization of the fuzzy set semi rings and the bipolar fuzzy ideals in semi rings and bipolar fuzzy ideals, respectively and the related properties are being examined by the authors. Assistant professor Recruitment process for higher education is regarded as a special case of personnel selection. Liang and M.J.Wang [11] study about the fuzzy multi criteria decision making [MCDM] algorithm for the purpose of personnel selection. Karsak [10] has presented the fuzzy MCDM approach based on the ideal and the anti ideal solutions for the selection of the most suitable candidate Z.Gunar [8] has developed the analytical hierarchy process [Attp] for the sake of personnel selection. M.Dog Devigen[6] has studied about the hybrid model based on the analytical network process [ANP] and has modified the technique for order preference by similarity to ideal solution for supporting the personnel selection process in the manufacturing systems. M.Sursun and E.E. Karsak [7]discusses the fuzzy MCDM approach by using Tops is with Tuples for the process of personnel selections. IT. Robertson and B.Smith [16] investigate the



role of top analysis, the contemporary models of work performance, and the set of criteria which has been employed in the personnel selection process.

#### SOME BASIC CONCEPTS OF BIPOLAR FUZZY SOFT SETS:

**Definition 2.1** A bipolar fuzzy subset (briefly, BF-subset), A in a non-empty set X is an object having the form  $A = \{(x, \mu_A^+(x), \mu_A^-(x) / x \in X\}$  where  $\mu_A^+: X \to [0,1]$  and  $\mu_A^-: X \to [-1,0]$ 

The positive membership degree  $\mu_A^+$  denote the satisfaction of an element x to the property corresponding to a BF – subset A and the negative membership degree  $\mu_A^-$  denotes the satisfaction degree of X to some implicit counter property of BF – subset A. Bipolar fuzzy sets and Intuitionist fuzzy set look similar to each other. However, they are different from each other.

**Definition 2.2**Let U be initial universe and F be a set of parameters. Let P (U) denote the power set of U and A be a non empty subset of F then  $F_A$  is called a soft set over U where  $F:A \rightarrow P(U)$  is a mapping from A into P(U).

**Definition 2.3**  $F_E$  is called the soft set over U if and only if F is a mapping of E into the set of all subsets of the set U.

**Definition 2.4** Let U be on initial Universe E be the set of parameter. A is subset of E. Define F:A $\rightarrow$ BFU, where BFU is the collection of all bipolar fuzzy subset of U, then(F,A) is said to be a bipolar fuzzy of soft set over U and it is denoted by

$$(F,A) = A = \{(x,\mu_e^+(x), \mu_e^-(x) / x \in U \text{ and } e \in A\}$$

**Example:** Let U=  $\{c_1, c_2, c_3\}$  be the set of 3 objects under consideration and E= $\{e_1=high, e_2=Low, e_3=Medium\}$  be the set of parameter and A= $\{e_1, e_2, e_3\}$  is subset of E then



**Definition 2.5**Let U be a Universe and E a set of attributes then, (U.E) is the collection of all bipolar fuzzy soft sets on U with attributes from E and is said to be bipolar fuzzy soft class.

**Definition 2.6**A bipolar fuzzy soft set (F,A) is said to be a null bipolar fuzzy soft set denoted by  $\phi$ , if for all  $e \in A$ , F(e) =  $\phi$ 

**Definition 2.7**A bipolar fuzzy soft set (F,A) is said to be an absolute bipolar fuzzy soft set, if for all  $e \in A$ , F(e) = BFU.

#### **RANKING METHODS FOR BFSNS**

In this subsection, we define the score function, accuracy function and hybrid score accuracy function of a BFSN and the ranking method for BFSNS.

**Definition 3.1** [Score function and accuracy function]

Let  $x = \langle P(x), N(x) \rangle$  be a BFSN. Then the score function and accuracy function of the BFSN can be presented respectively as follows.

Score function 
$$S(x) = \frac{1+P(x)-N(x)}{2}$$
, for  $S(x) \in [-1,1] \rightarrow (1)$   
Accuracy function  $h(x) = \frac{2+P(x)-N(x)}{3}$ , for  $h(x) \in [-1,1] \rightarrow (2)$ 

for the score function of a BFSN 'x' if the positive membership p(x) is bigger and the negative membership N(x) is Lower, then the score value of BFSN is a greater for the accuracy function of a BFSN 'x' if the sum of P(x) and 1 - N(x) is greater than the statement is more affirmative. That is the accuracy of the BFSN 'x' is higher. Based on score and accuracy functions for BFSNS, two theorems are stated below.



**Theorem 3.1:** For any two BFSNS  $x_1$  and  $x_2$  if  $x_1 > x_2$ , then  $S(x_1) > S(x_2)$ 

**Theorem 3.2:** For any two BFSNS  $x_1$  and  $x_2$  if  $S(x_1) = S(x_2)$  and  $x_1 \ge x_2$ , then  $h(x_1) \ge h(x_2)$  Based on theorems 3.1 and 3.2, a ranking method between BFSNS can be given by the following definition.

**Definition 3.2**Let  $x_1$  and  $x_2$  is two BFSNS then the ranking method can be defined as follows. (i) if  $S(x_1) > S(x_2)$ , then  $x_1 > x_2$ , (ii) if  $S(x_1) = S(x_2)$  and  $h(x_1) \ge h(x_2)$ , then  $x_1 \ge x_2$ 

### IMPORTANT PARAMETERS OF THE TERM STATED IN THE PROBLEM

- (i) Academic performance: This implies the percentage of marks (if grades are given, transform it into marks) obtained in post graduate examinations.
- (ii) **Teaching Aptitude:** Degree of knowledge in strategies of institution and information communication technology.
- (iii) **Subject Knowledge:** Degree of knowledge of a person in his/her respective field of study to be delivered during his/her instruction.
- (iv) **Research experience:** Research experience of a person implies his/her contribution of new knowledge in the form of publication is reputed peer reviewed journals with highly impact factor.
- (v) **Leadership quality:** A leadership quality of a person to maintain and control the team members and giving effectiveness through their academic.

## GROUP DECISION MAKING METHOD IN BIPOLAR FUZZY SOFT SETTING

In a multi criteria group decision making problem, let  $A=\{A_1,A_2,...,A_m\}$  be a set of alternatives and  $C=\{c_1,c_2,...,c_n\}$  be a set of attributes. In the group decision process under bipolar fuzzy soft environment if a group of t decision makers or experts is required in the evaluation process, then the  $k^{th}$  decision maker can provide the evaluation information of the alternative  $A_i$ , (i=1,2,...,m) on the attribute  $c_j$  (j=1,2,...,n) which is represented by the form of a BFSNS

$$A_{i}^{k} = \{ < c_{j} P_{Ai}^{k} (c_{j}), N_{Ai}^{k} (c_{j}) > / c_{j} \in C \}$$

When  $P_{Ai}^{k}$  (c<sub>j</sub>)  $\in$  [0,1] and  $N_{Ai}^{k}$  (c<sub>j</sub>)  $\in$  [-1,0] for k = 1,2,....,n, i=1,2,...,n for convenience,  $X_{ij}^{k} = \langle P_{ij}^{k} N_{ij}^{k} \rangle$  is denoted as BFSNS. $A_{i}^{k}$ .(k = 1,2,...,t, j=1,2,...,n, i=1,2,...,n), therefore, we can get the K<sup>th</sup>Bipolar fuzzy soft decision matrix.D<sup>k</sup> =  $(A_{ij}^{k})_{mxn}$  (k = 1,2,...,t) then, the group decision – making method is described as follows.

## **ALGORITHM-1**

**Step-1: Calculate hybrid score accuracy matrix :** The hybrid score – accuracy matrix  $Y^{k} = (Y_{ij}^{k})_{m \times n}$  (k = 1,2,.....t, j=1,2,....n, i=1,2,....m), is obtained from the decision matrix  $D^{k}$  by the following formula.

$$\left(Y_{ij}^{k}\right) = \frac{1}{2}\alpha \left(1 + P_{ij}^{k} - N_{ij}^{k}\right) + \frac{1}{3}\left(1 - \alpha\right) \left(2 + P_{ij}^{k} - N_{ij}^{k}\right) \longrightarrow (3)$$

**Step-2:** Calculate the average matrix: From step-1, the average matrix  $Y^* = (Y_{ij}^*)_{m \times n}$  (k = 1,2,.....n, i=1,2,....n, i=1,2,....n), is calculated by

$$Y_{ij}^* = \frac{1}{t} \sum_{k=1}^{t} (Y_{ij}^k) \rightarrow \qquad (4)$$

Step-3: The collection correlation coefficient between Y<sup>k</sup> (k=1,2,.....t) and Y represents as follows

$$\rho_{k=} \sum_{i=1}^{m} \frac{\sum\limits_{j=1}^{\Sigma} Y_{ij}^{k} Y_{ij}^{*}}{\sqrt{\sum\limits_{j=1}^{n} (Y_{ij}^{k})^{2}} \sqrt{\sum\limits_{j=1}^{n} (Y_{ij}^{*})^{2}}} \longrightarrow (5)$$

Step-4: Determination of Decision makers weights: The weight model for decision makers can be defined as:

$$\lambda_{k} = \frac{\rho_{k}}{\sum_{k=1}^{t-1} \rho_{k}} \longrightarrow (6)$$
  
Where  $0 \le \lambda_{k} \le 1$ , and  $\sum_{k=1}^{t} \lambda_{k} = 1$  for  $k = 1, 2, \dots, t$ 

Step-5: Calculate collective hybrid score - accuracy matrix: For the weight vector



 $\lambda = (\lambda_1, \lambda_2, \lambda_3, \dots, \lambda_k)$  of decision makers obtained from step-4, we collect all the individual hybrid score accuracy matrices of  $Y^k = (Y_{ij}^k)_{m \times n}$  (k = 1,2,...,i=1,2,...,n,i=1,2,...,m), in to a collective hybrid score accuracy matrix  $Y = (Y_{ij})_{m \times n}$  by the following formula

$$Y_{ij} = \sum_{k=1}^{l} \lambda_k Y_{ij}^k \longrightarrow$$
(7)

**Step-6: Weight model for attributes:** To determine the weight vector of the attributesJ.Ye [14, 15], introduced the following optimization method

$$\operatorname{Max} W = \frac{1}{m} \sum_{j=1}^{n} \sum_{i=1}^{m} W_{j} Y_{ij}$$

$$\operatorname{Subject to} \sum_{j=1}^{n} W_{j} = 1 \text{ and } W_{j} > 0 \longrightarrow (8)$$

This is a linear programming problem which can be easily solved to determine the weightvector of the attributes  $W = (W_1, W_2, W_3, \dots, W_n)^T$ .

**Step-7: Ranking alternatives :** To rank alternative, we can sum all values is each row of the collective hybrid score – accuracy matrix corresponding to the attributes weights by the overall weighted hybrid score – accuracy value of each alternative  $A_i$  (i=1,2,.....m)

$$M(A_i) = \sum_{j=1}^{N} W_j Y_{ij} \longrightarrow$$
(9)According to the

overall hybrid score accuracy values of  $M(A_i)$  (i=1,2,....m). We can rank alternative  $A_i$  (i=1,2,....m) in descending order and choose the best one.

#### NUMERICAL EXAMPLE

Suppose that a Monomania Sundaranar University is going to recruit in the post of Assistant Professors for a particular subject. After initial screening, five candidates (that is alternatives)  $A_1$ ,  $A_2$ ,  $A_3$ ,  $A_4$ ,  $A_5$  remain for further evaluation.

A committee of four decision makers or exports  $D_1, D_2, D_3, D_4$  has been formed to conduct the interview and select the most appropriate candidate, five criteria obtained from expert opinions, namely, Academic performance - (C<sub>1</sub>), Subject knowledge - (C<sub>2</sub>), Teaching aptitude - (C<sub>3</sub>), Research Experience- (C<sub>4</sub>), Leadership Quality- (C<sub>5</sub>) are considered for recruitment criteria of four experts are required in the evaluation process, then the five possible alternatives A<sub>i</sub> (i=1,2,3,....5) are evaluated by the form of BFSNS. Under the five attributes on the fuzzy concept **"Excellence"** thus the four bipolar valued fuzzy soft decision matrices can be obtained from the four experts and expressed respectively as follows (See table 1.2.2.4).

(See table 1,2,3,4).

| Table 1 | Bipolar | valued fu | zzy soft | decision | matrix | ( <b>D</b> <sub>1</sub> ): |
|---------|---------|-----------|----------|----------|--------|----------------------------|
|---------|---------|-----------|----------|----------|--------|----------------------------|

|                | <b>C</b> <sub>1</sub> | <b>C</b> <sub>2</sub> | C <sub>3</sub> | C4          | C <sub>5</sub> |
|----------------|-----------------------|-----------------------|----------------|-------------|----------------|
| $A_1$          | [0.8, -0.4]           | [0.6, -0.3]           | [0.7, -0.2]    | [0.5, -0.3] | [0.4, -0.3]    |
| $A_2$          | [0.8,-0.6]            | [0.6, -0.5]           | [0.7, -0.4]    | [0.5, -0.2] | [0.4, -0.2]    |
| A <sub>3</sub> | [0.8, -0.3]           | [0.6, -0.4]           | [0.7, -0.1]    | [0.5, -0.1] | [0.4, -0.1]    |
| $A_4$          | [0.8, -0.1]           | [0.6, -0.2]           | [0.7, -0.3]    | [0.5, -0.4] | [0.4, -0.4]    |
| $A_5$          | [0.8, -0.2]           | [0.6, -0.1]           | [0.7, -0.1]    | [0.5, -0.3] | [0.4, -0.3]    |

| Table 2 Bipolar valued fuzz | y soft decision matrix | ( <b>D</b> <sub>2</sub> ): |
|-----------------------------|------------------------|----------------------------|
|-----------------------------|------------------------|----------------------------|

|                | <b>C</b> <sub>1</sub> | $C_2$       | C <sub>3</sub> | <b>C</b> <sub>4</sub> | C <sub>5</sub> |
|----------------|-----------------------|-------------|----------------|-----------------------|----------------|
| $A_1$          | [0.6, -0.4]           | [0.7, -0.4] | [0.5, -0.3]    | [0.4, -0.3]           | [0.6, -0.5]    |
| $A_2$          | [0.6, -0.3]           | [0.7, -0.5] | [0.5, -0.4]    | [0.4, -0.2]           | [0.6, -0.4]    |
| A <sub>3</sub> | [0.6, -0.2]           | [0.7, -0.3] | [0.5, -0.3]    | [0.4, -0.1]           | [0.6, -0.3]    |
| $A_4$          | [0.6, -0.1]           | [0.7, -0.1] | [0.5, -0.1]    | [0.4, -0.2]           | [0.6, -0.2]    |
| $A_5$          | [0.6, -0.1]           | [0.7, -0.2] | [0.5, -0.2]    | [0.4, -0.1]           | [0.6, -0.1]    |



|                | <b>C</b> <sub>1</sub> | <b>C</b> <sub>2</sub> | C <sub>3</sub> | C <sub>4</sub> | C <sub>5</sub> |
|----------------|-----------------------|-----------------------|----------------|----------------|----------------|
| $A_1$          | [0.4, -0.2]           | [0.5, -0.4]           | [0.6, -0.5]    | [0.7, -0.6]    | [0.8, -0.5]    |
| $A_2$          | [0.4, -0.1]           | [0.5, -0.3]           | [0.6, -0.3]    | [0.7, -0.5]    | [0.8, -0.6]    |
| A <sub>3</sub> | [0.4, -0.3]           | [0.5, -0.2]           | [0.6, -0.2]    | [0.7, -0.4]    | [0.8, -0.5]    |
| $A_4$          | [0.4, -0.2]           | [0.5, -0.1]           | [0.6, -0.1]    | [0.7, -0.3]    | [0.8, -0.4]    |
| A <sub>5</sub> | [0.4, -0.1]           | [0.5, -0.3]           | [0.6, -0.5]    | [0.7, -0.2]    | [0.8, -0.3]    |

Table 3: Bipolar valued fuzzy soft decision matrix(D3)

Table 4 Bipolar valued fuzzy soft decision matrix(D4)

|                       | C <sub>1</sub> | C <sub>2</sub> | C <sub>3</sub> | C4          | C <sub>5</sub> |
|-----------------------|----------------|----------------|----------------|-------------|----------------|
| $A_1$                 | [0.6, -0.5]    | [0.7, -0.6]    | [0.8, -0.6]    | [0.5, -0.4] | [0.4, -0.1]    |
| $A_2$                 | [0.6, -0.4]    | [0.7, -0.5]    | [0.8, -0.5]    | [0.5, -0.3] | [0.4, -0.3]    |
| <b>A</b> <sub>3</sub> | [0.6, -0.3]    | [0.7, -0.4]    | [0.8, -0.6]    | [0.5, -0.2] | [0.4, -0.2]    |
| $A_4$                 | [0.6, -0.4]    | [0.7, -0.3]    | [0.8, -0.5]    | [0.5, -0.1] | [0.4, -0.3]    |
| A <sub>5</sub>        | [0.6, -0.5]    | [0.7, -0.2]    | [0.8, -0.4]    | [0.5, -0.3] | [0.4, -0.1]    |

# Step -1: Form the Hybrid Score Accuracy Matrix for D<sub>1</sub>

| Table – 5: Form | the Hybrid Score | Accuracy Matrix for D <sub>1</sub> |
|-----------------|------------------|------------------------------------|
|                 | •                | · · ·                              |

|                       | C <sub>1</sub> | C <sub>2</sub> | C <sub>3</sub> | C <sub>4</sub> | C <sub>5</sub> |
|-----------------------|----------------|----------------|----------------|----------------|----------------|
| A <sub>1</sub>        | 1.083          | 0.958          | 0.958          | 0.916          | 0.875          |
| <b>A</b> <sub>2</sub> | 1.166          | 1.066          | 1.041          | 0.875          | 0.833          |
| A <sub>3</sub>        | 1.0416         | 1.000          | 0.9166         | 0.833          | 0.7916         |
| A <sub>4</sub>        | 0.958          | 0.916          | 1.000          | 0.958          | 0.875          |
| A <sub>5</sub>        | 1.000          | 0.875          | 1.008          | 0.916          | 0.833          |

Table -6: Form the Hybrid Score Accuracy Matrix for D<sub>2</sub>

|                | C <sub>1</sub> | C <sub>2</sub> | C <sub>3</sub> | C <sub>4</sub> | C <sub>5</sub> |
|----------------|----------------|----------------|----------------|----------------|----------------|
| A <sub>1</sub> | 1.0416         | 0.916          | 1.041          | 0.875          | 1.166          |
| A <sub>2</sub> | 1.083          | 0.875          | 0.958          | 0.833          | 1.125          |
| A <sub>3</sub> | 1.000          | 0.958          | 1.000          | 0.791          | 1.083          |
| A <sub>4</sub> | 0.958          | 0.916          | 0.916          | 0.875          | 1.041          |
| A <sub>5</sub> | 0.916          | 0.875          | 0.875          | 0.791          | 1.000          |

| Table – 7: Form | the Hybrid | <b>Score Accuracy</b> | Matrix for D <sub>3</sub> |
|-----------------|------------|-----------------------|---------------------------|
|-----------------|------------|-----------------------|---------------------------|

|                | C <sub>1</sub> | C <sub>2</sub> | C <sub>3</sub> | C4    | C <sub>5</sub> |
|----------------|----------------|----------------|----------------|-------|----------------|
| A <sub>1</sub> | 0.833          | 0.958          | 1.041          | 1.125 | 1.125          |
| $A_2$          | 0.791          | 0.916          | 0.958          | 1.083 | 1.166          |
| A <sub>3</sub> | 0.875          | 0.875          | 0.916          | 1.041 | 1.125          |
| A <sub>4</sub> | 0.833          | 0.833          | 0.875          | 1.000 | 1.083          |
| A <sub>5</sub> | 0.791          | 0.916          | 1.041          | 0.958 | 1.0.41         |

| Table – 8 | : Form     | the H | vbrid | Score | Accuracy | Matrix     | for D₄ |
|-----------|------------|-------|-------|-------|----------|------------|--------|
| I able 0  | • 1 01 111 | une m | JULIU | Deore | necuracy | TATCELL IV | 101 04 |

|                | C <sub>1</sub> | $C_2$ | C <sub>3</sub> | C <sub>4</sub> | C <sub>5</sub> |
|----------------|----------------|-------|----------------|----------------|----------------|
| A <sub>1</sub> | 1.041          | 1.125 | 1.166          | 0.958          | 0.791          |
| $A_2$          | 1.000          | 1.083 | 1.125          | 0.916          | 0.875          |



| A <sub>3</sub> | 0.958 | 1.041 | 1.166 | 0.875 | 0.833 |
|----------------|-------|-------|-------|-------|-------|
| $A_4$          | 1.000 | 1.000 | 1.125 | 0.833 | 0.875 |
| A <sub>5</sub> | 1.041 | 0.958 | 1.083 | 1.000 | 0.916 |

Step-2: Calculate the average matrix: From Step 2, we can calculate the average matrix by using the formula

$$Y_{ij}^* = \frac{1}{t} \sum_{k=1}^{t} (Y_{ij}^k)$$

## **Table Calculation**

|                       | C <sub>1</sub> | C <sub>2</sub> | C <sub>3</sub> | C <sub>4</sub> |
|-----------------------|----------------|----------------|----------------|----------------|
| A <sub>1</sub>        | 0.958          | 1.007          | 1.016          | 1.016          |
| A <sub>2</sub>        | 0.996          | 0.974          | 0.982          | 0.999          |
| A <sub>3</sub>        | 0.916          | 0.966          | 0.966          | 0.974          |
| A <sub>4</sub>        | 0.941          | 0.941          | 0.924          | 0.966          |
| <b>A</b> <sub>5</sub> | 0.926          | 0.891          | 0.949          | 0.999          |

Step-3: Collection of Correlation coefficient : The Correlation coefficient



Using this formula we obtain the values of

 $\rho_{1}=4.981, \rho_{2}=4.979, \rho_{3}=4.981, \rho_{4}=4.958$ 

Step-4: Determination of Decision makers weights

$$\lambda_k = \frac{\rho_k}{t-1} \\ \sum_{\substack{k=1}}^{k} \rho_k$$

In this Equation we determine the weight decision four makers as follows.  $\lambda_1 = 0.2507, \quad \lambda_2 = 0.2501, \quad \lambda_3 = 0.2503 \quad \lambda_4 = 0.2491$ 

**Step-5:** Calculate collective hybrid score – accuracy matrix

$$Y_{ij} = \sum_{k=1}^{l} \lambda_k Y_{ij}^k$$

Using this formula we can obtain the hybrids score accuracy matrix.

|                | <b>C</b> <sub>1</sub> | <b>C</b> <sub>2</sub> | C <sub>3</sub> | C4     | C <sub>5</sub> |
|----------------|-----------------------|-----------------------|----------------|--------|----------------|
| A <sub>1</sub> | 0.998                 | 0.9892                | 1.0515         | 0.9687 | 0.9896         |
| A <sub>2</sub> | 1.0103                | 0.9851                | 1.0206         | 0.9269 | 1.000          |
| A <sub>3</sub> | 0.9689                | 0.9686                | 0.9996         | 0.8852 | 0.9584         |
| A <sub>4</sub> | 0.9374                | 0.9163                | 0.9063         | 0.9168 | 0.9688         |
| A <sub>5</sub> | 0.9374                | 0.9061                | 1.001          | 0.9163 | 0.9476         |

**Step-6: Weight model for attributes:** Assume that the information above attributes weights is incompletely known weight vectors  $0.1 \le w_1 \le 0.2$ ,  $0.1 \le w_2 \le 0.2$ ,  $0.1 \le w_3 \le 0.2$ ,  $0.1 \le w_4 \le 0.2$ , which is given decision makers. By linear programming model in equation (8) we can obtained the weight vectors W=[0.2, 0.2, 0.2, 0.2, 0.2]

**Step- 7: Ranking Alternative :** From The above weighted vectors the ranking alternatives is given by M (A<sub>i</sub>), (i=1,2,....5) as follows  $M(A_1) = 0.9997$ ,  $M(A_2) = 0.9885$ ,  $M(A_3) = 0.9554$ ,  $M(A_4) = 0.9291$ ,  $M(A_5) = 0.9414$ . The preference for ranking order of alternatives are  $A_1 > A_2 > A_3 > A_5 > A_4$ . Hence  $A_1$  is the best assistant professor for the selection in Government sectors. By similar computation procedures, we can get various different ways for different  $\alpha$  values.



# CONCLUSION

In this paper we employ the scope and accuracy function, hybrid score accuracy functions of BFSNS to recruit best professor for higher education, under bipolar fuzzy soft Environment, where the weights of decision makers are completely unknown and the weights of attributes are incompletely known.

## SCOPE FOR FURTHER RESEARCH

In future, one can obtain the extension and application of the methods to other domains, such as best row material selection for industries.

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